

**A Thesis for the degree of Doctor of Philosophy**

**Unsteady Computational Simulation of Ice  
Protection Systems in Aircraft Icing using the  
Conjugate Heat Transfer Method**

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Esmail Esmailifar  
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# Dedication

I dedicate this thesis to my beloved wife, Mina, whose unwavering love, support, and patience have been my constant source of strength throughout this journey.

I also want to thank my parents and sisters, who have always loved me unconditionally.

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# **Abstract**

## **Unsteady Computational Simulation of Ice Protection Systems in Aircraft Icing using the Conjugate Heat Transfer Method**

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In-flight icing occurs when an aircraft or rotorcraft fly through icing clouds, and supercooled water droplets impact the surface of the flying vehicle. Ice accumulation on the wing, engine inlet, cockpit windows, and pitot tube of aircraft can degrade aerodynamic performance and handling quality. Designing reliable and efficient ice protection systems is essential to mitigate the adverse effect of ice accretion and ensure a safe flight. Electrothermal ice protection systems have become popular due to their compatibility with more electric aircraft trends and composite structures. Moreover, it can be utilized as a hybrid ice protection system in conjunction with emerging superhydrophobic coating, which can save a significant amount of energy.

Employing experimental tests to design ice protection systems is limited due to the high cost, lack of facilities, and scalability issues. Developing accurate and reliable computational solvers can significantly decrease costs and speed up the design and certification processes. In this study, a unified framework was developed to simulate electrothermal ice protection systems in aircraft icing. The electrothermal ice protection system framework comprises several solvers, including a compressible Navier-Stokes-Fourier airflow solver, a Eulerian

droplet impingement solver, an unsteady ice accretion/melting solver, and a heat conduction solver. These solvers are formulated using partial differential equations and implemented within a unified finite volume framework. This approach allows for the use of a single grid system, eliminating the need for additional grid generation specifically for the ice layer.

Ice and conduction solvers were tightly coupled using the conjugate heat transfer method, where the runback water and ice domain were linked to the multilayer solid domain by exchanging thermal boundary conditions at the interface. The electrothermal de-icing solver was validated using experimental data from electrothermal de-icing tests conducted in the NASA Lewis Icing Research Tunnel. The de-icing process was also studied by analyzing the runback water film, ice accretion/melting, and temperature distribution on the surface.

Moreover, the air solver was loosely coupled with ice/conduction solvers to update the airflow based on the transient wall temperature distribution calculated in the ice/conduction solvers. Interestingly, the anti-icing results obtained by the loosely coupled solver were also compared with the decoupled solver and experimental data for different anti-icing regimes. Results obtained by coupled solver are in better agreement with experimental data compared to the decoupled solver, especially in the leading edge's aft region. Finally, a novel framework was developed to evaluate the required heat load at running wet, evaporative, and fully evaporative anti-icing modes.

In order to simulate ice accretion on superhydrophobic surfaces, two modifications were applied to the droplet and ice solvers. First, the semi-empirical supercooled large droplet model, which was developed to consider the effects of droplet/wall interaction, was modified to consider the wettability effects on collection efficiency. Second, the lubrication theory equations were revisited to modify the shallow water icing model considering the partial slip boundary conditions. Results show that the droplet deposition rate decreases by increasing the

surface contact angle. Moreover, increasing the contact angle can result in different ice-type formations at the same atmospheric and icing conditions.